

## Goals:

- \* kinematics
- \* anthropometry
- \* kinetics

} gait cycle

# Movement Analysis

## Anatomical Terms

- \* medial - lateral

medial - near middle  
lateral - away middle

- \* Anterior - posterior

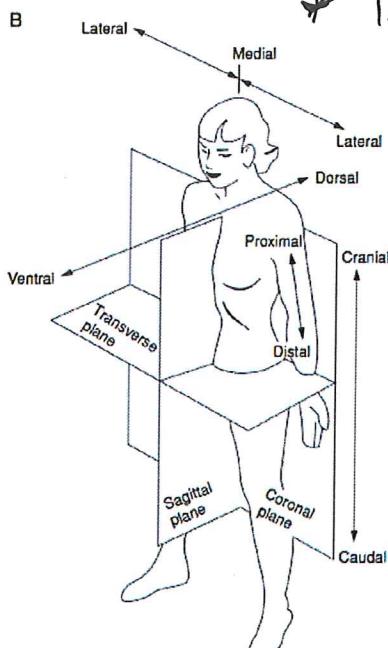
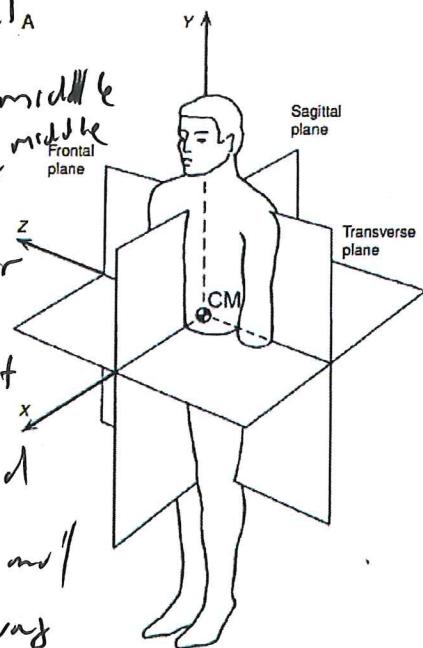
- Anterior  
- in front of

Posterior  
- behind

- \* Distal Proximal

\* distant away  
from trunk

\* proximal towards trunk



- \* Superior - Inferior

\* Superior - above

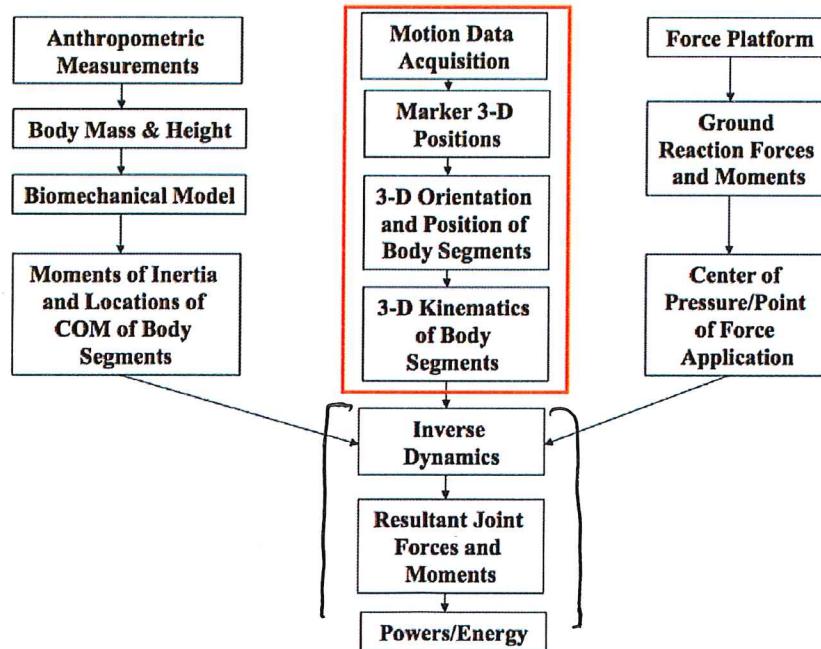
\* Inferior - below

- \* Cranial - (head)

~~Lateral~~  
towards head

Caudal:  
toward  
feet

## Overview of Human Movement Analysis



## Motion Capture Techniques

### \* Tachometers

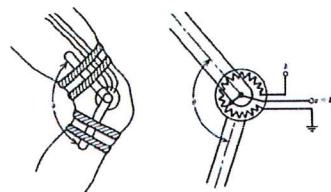
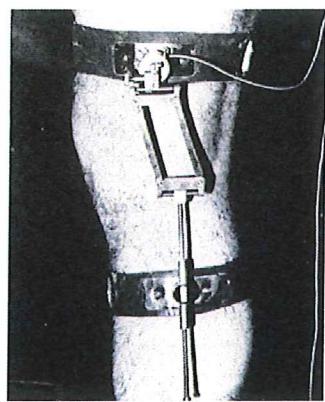
#### \* electrical potentiometer

##### Advantages:

- inexpensive, easy

##### Disadvantages:

- relative motion
- put a lot on, encumber motion.



### \* IMU (acc. + gyroscope)

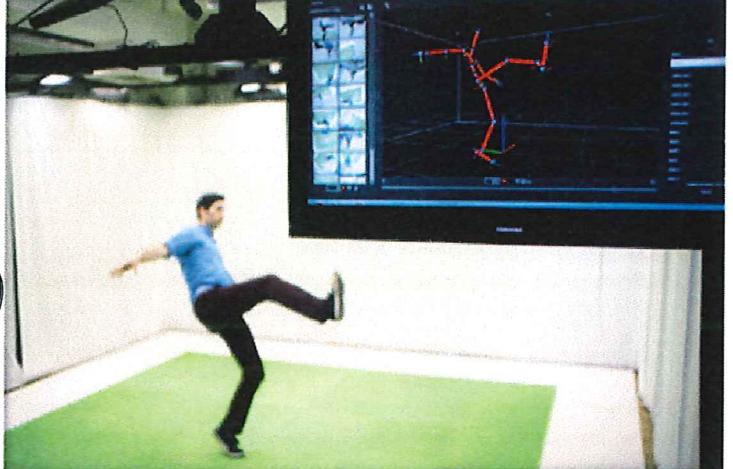
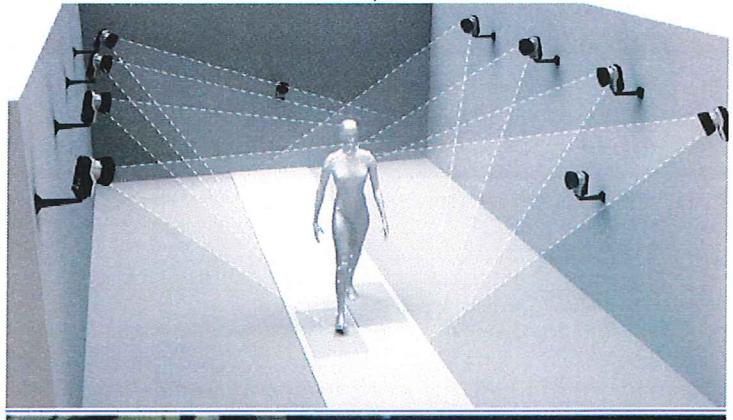
##### Advantages:

- relative inexpensive

##### Disadvantages:

- noisy

Winter, 2009



### \* Retro-reflective markers

#### \* strobe of IR

- reflect light back from markers

#### \* usually 6-12 cameras

#### \* specialized software

#### \* marker tech.

##### Advantages: relatively accurate (1-2mm)

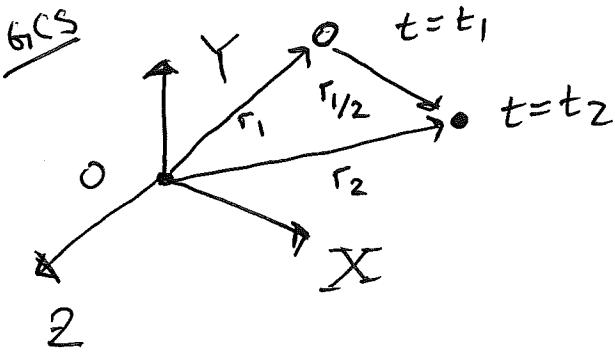
##### disadv.: expensive

- skin motion artifacts

## Kinematics Definition

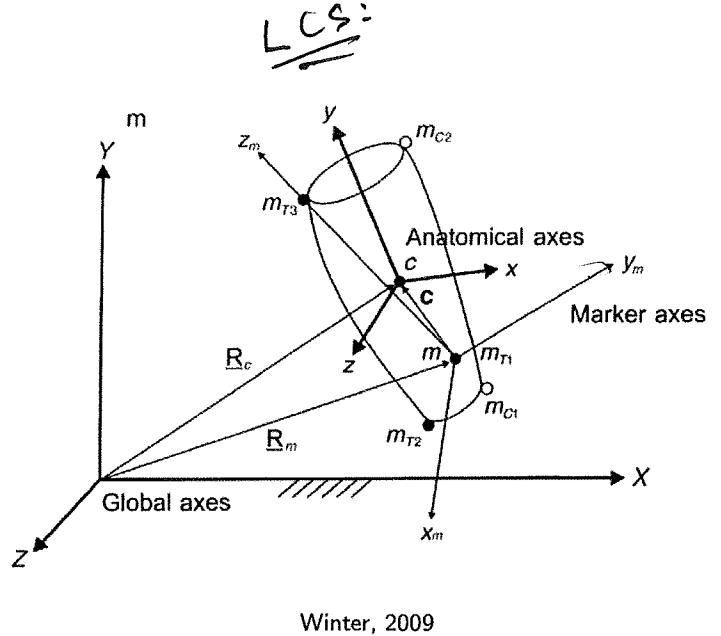
Study of motion w/o regard to force.

## Kinematics of a Rigid Body Segments

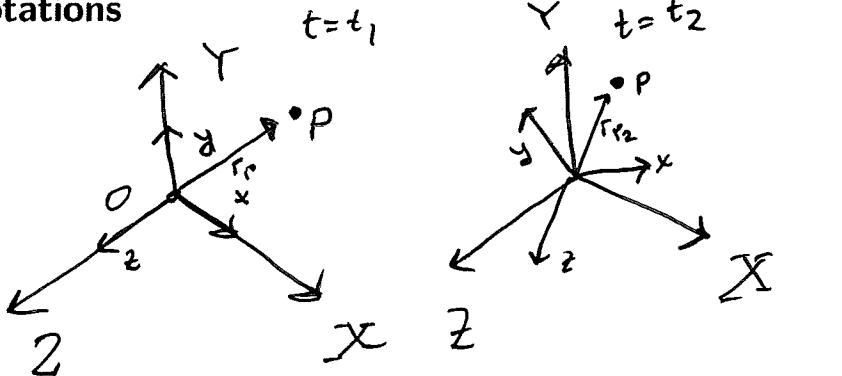


$$\begin{aligned} \mathbf{r}_1 &= x \hat{i} + y \hat{j} + z \hat{k} && \text{Position vectors} \\ \mathbf{r}_2 &= \begin{bmatrix} x \\ y \\ z \end{bmatrix} && \\ \mathbf{r}_{1/2} &= \mathbf{r}_2 - \mathbf{r}_1 && \text{displacement} \end{aligned}$$

Translations



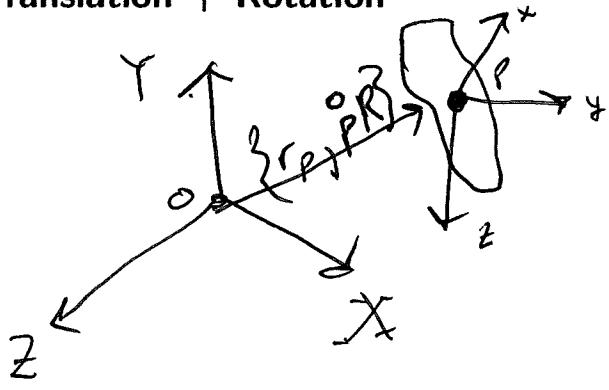
Rotations



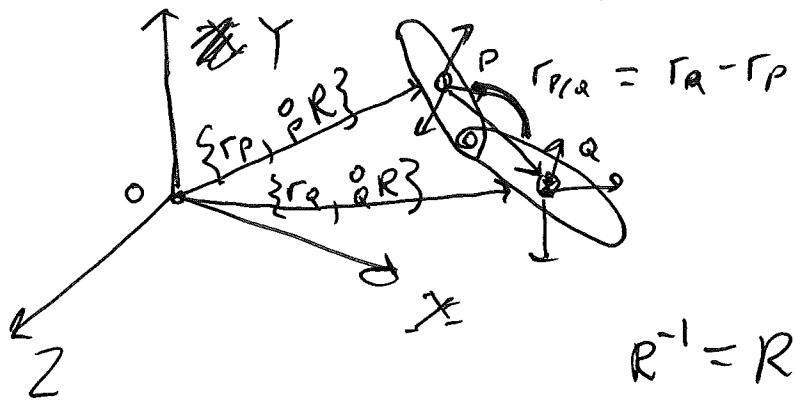
$$r_{P2} = R \ r_P$$

$\theta$

Translation + Rotation



## Determining Joint Kinematics (Angles)

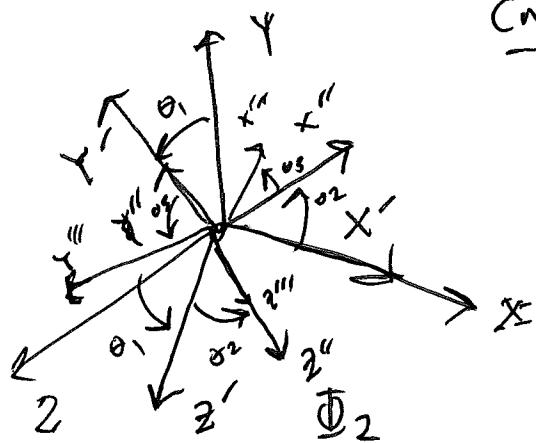


$$\begin{aligned} {}^P_Q R &= \{{}^P_R\}^{-1}({}^Q_R) \\ &= {}^P_R {}^Q_R \\ &= {}^P_Q R \end{aligned}$$

$$R^{-1} = R^T$$

$$({}^O_Q R)^{-1} = {}^Q_O R = {}^Q_R^T$$

### Rotational Matrices



Cardan —  $X - Y - Z$

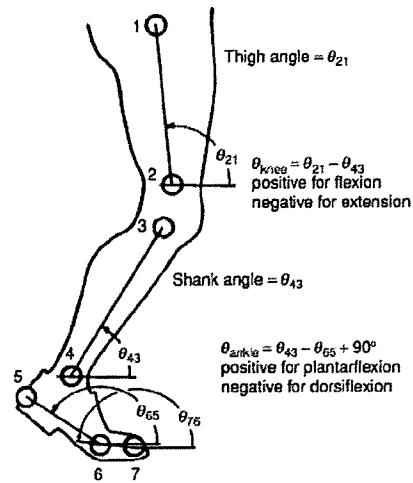
$$\theta_1 \quad \theta_2 \quad \theta_3$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix}' = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_1 & s_1 \\ 0 & -s_1 & c_1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix}''' = \begin{bmatrix} c_2 & 0 & -s_2 \\ 0 & 1 & 0 \\ s_2 & 0 & c_2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}'$$

### Sagittal Plane Angles

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix}''' = \begin{bmatrix} c_3 & s_3 & 0 \\ -s_3 & c_3 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}''$$

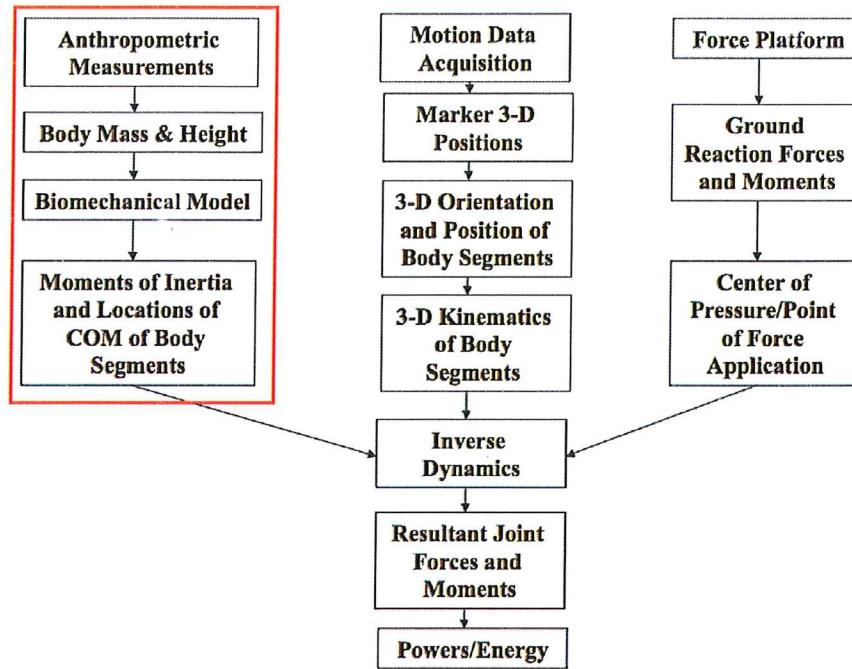


Winter, 2009

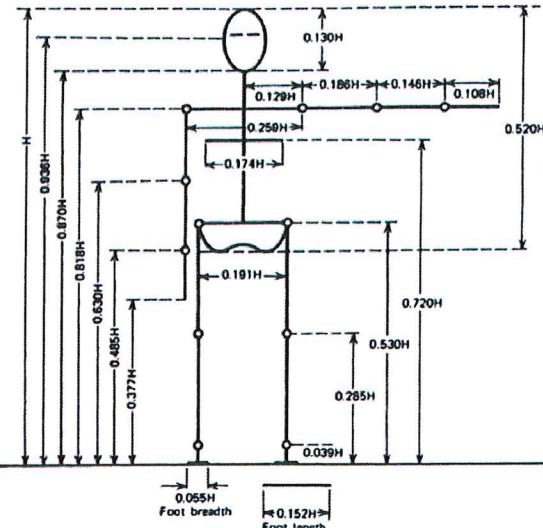
$$\begin{bmatrix} x \\ y \\ z \end{bmatrix}''' = \Phi_3(\Phi_2(\Phi_1 \begin{bmatrix} x \\ y \\ z \end{bmatrix}))$$

R

# Overview of Human Movement Analysis



Ledoux



## Anthropometry Definition

\* measurement of human individuals  
Segment Dimensions

\* Mass is Inertia

## Moment of Inertia

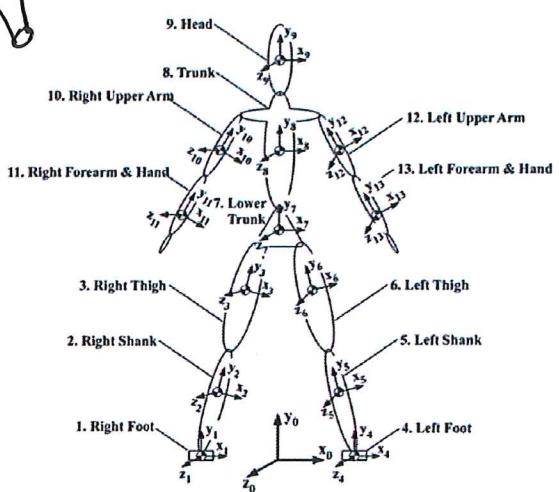
Inertia?

→ resistance to movement

$$I_0 = \sum m_i x_i^2$$

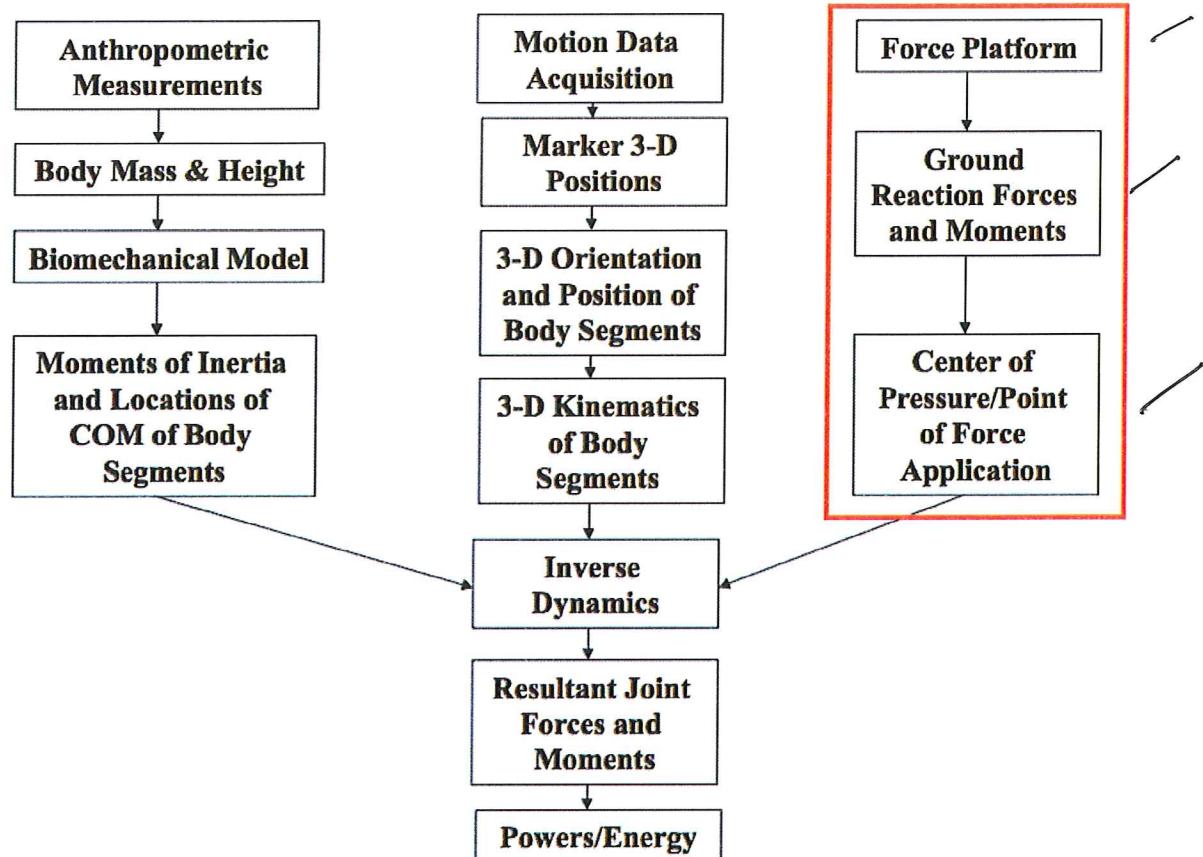
$$I = \sum m_i x_i^2$$

$$J = \int x^2 dm$$



Winter, 2009

# Overview of Human Movement Analysis



Ledoux

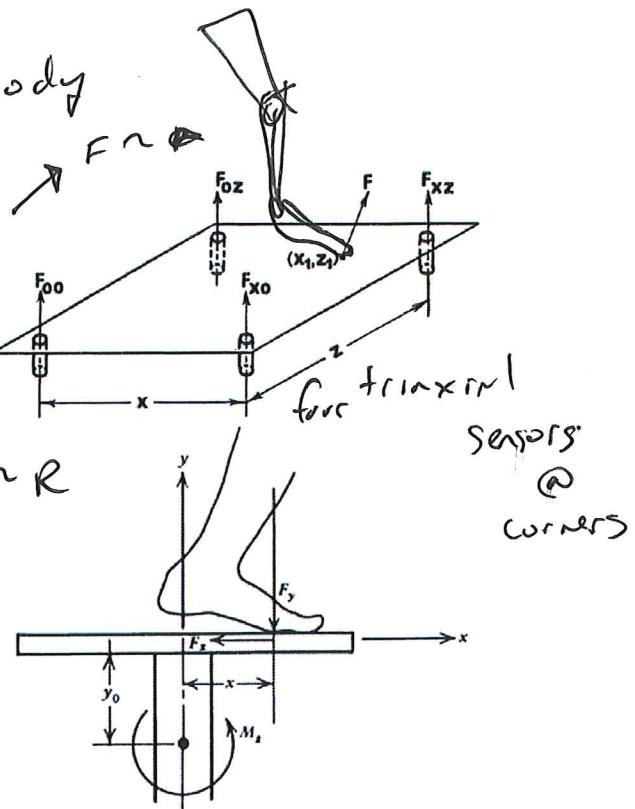
## Kinetics Definition

Study of forces on a body

## Types of Force Plates

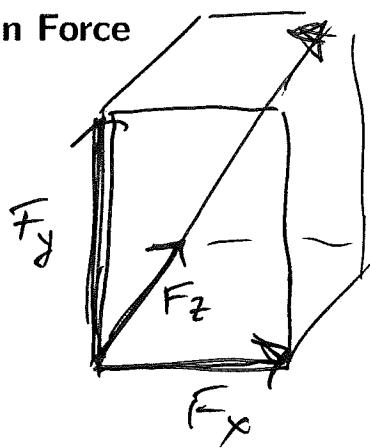
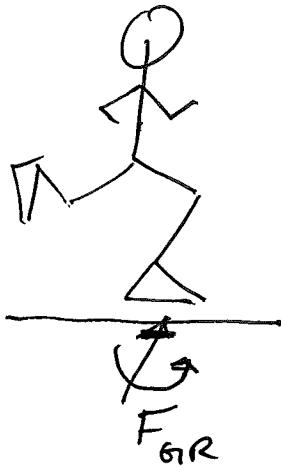
two types sensors: \* piezoelectric

\* strain gauge based



Winter, 2009

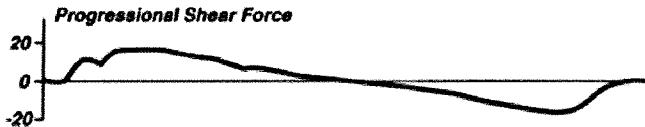
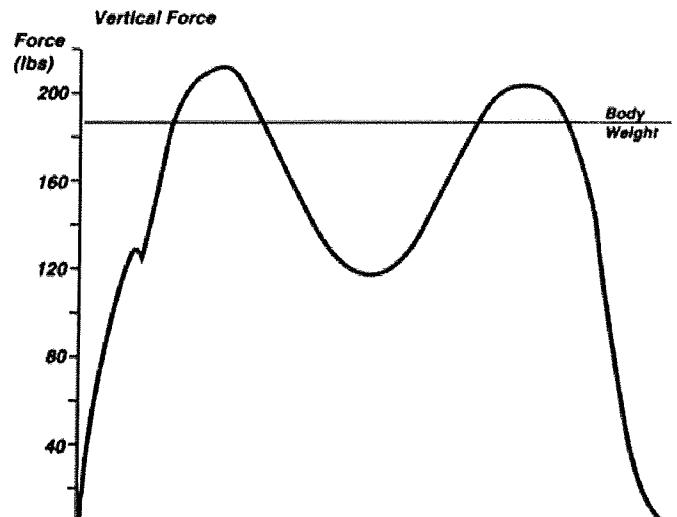
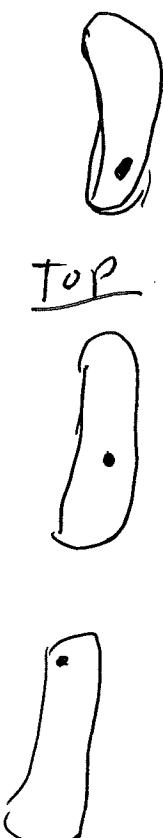
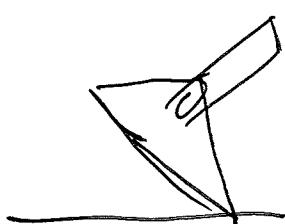
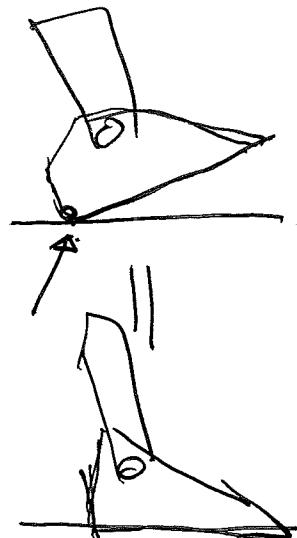
## Ground Reaction Force



$$F_y = \sum_{i=1}^n m_i ((a_{f_i} + g))$$

↓

## Center of Pressure

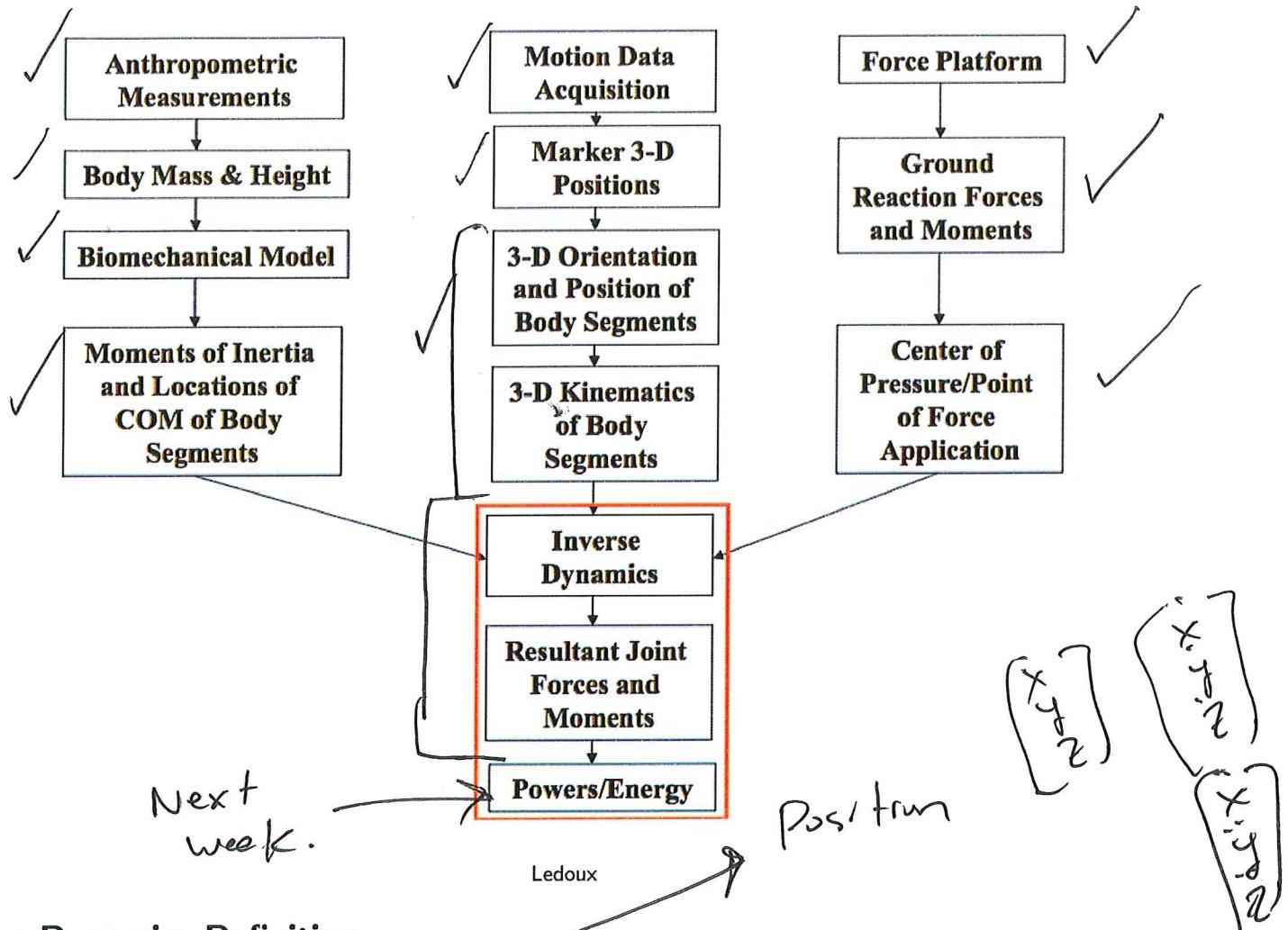


Ledoux

COP  
progression

↓  
a lot of  
climat  
applications

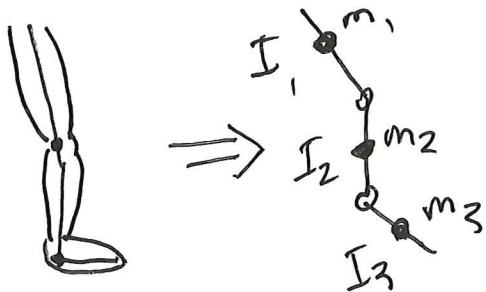
## Overview of Human Movement Analysis



### Inverse Dynamics Definition

Given the (kinematics)  
(kinetic) → solve for joint forces

### Link Segment Model



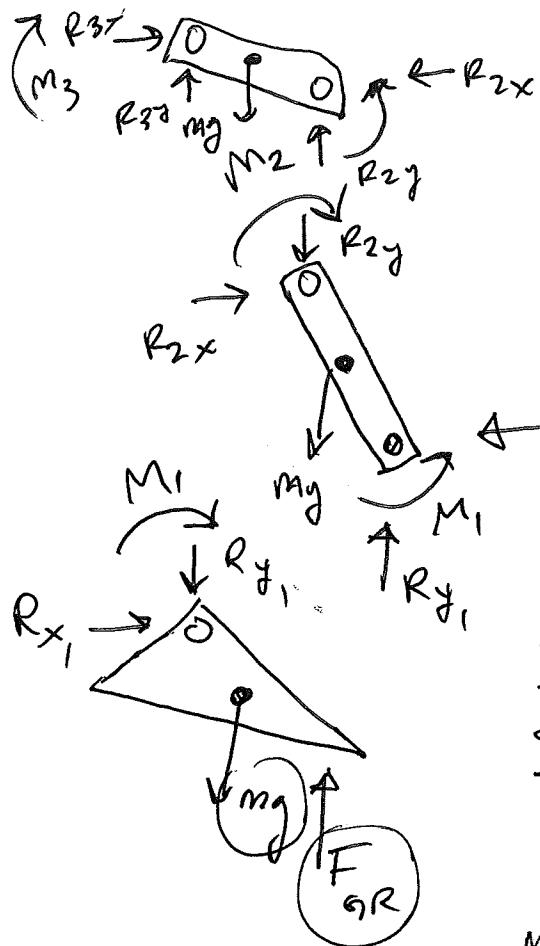
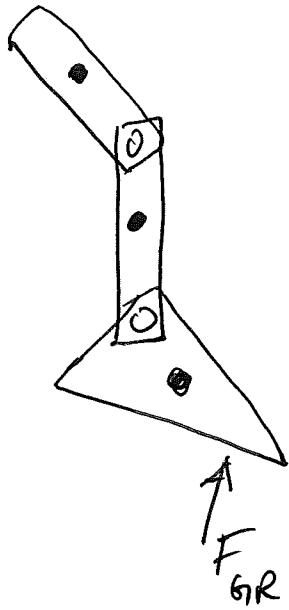
### Assumptions

- ① each segment has fixed mass @ COM
- ② COM remains fixed
- ③ joints are modeled as hinges
- ④ Moment of Inertia steps constant
- ⑤ length of segment is fixed

### Forces Involved

- ① gravity ( $mg$ )
- ② GRF + External forces
- ③ muscle forces

## Joint Reaction Forces



$$\sum M = I \alpha$$

$$\sum F_y = m a_y$$

$$\sum F_x = m a_x$$

## 3D Example

$$\sum F_x = m a_x$$

$$\sum F_y = m a_y$$

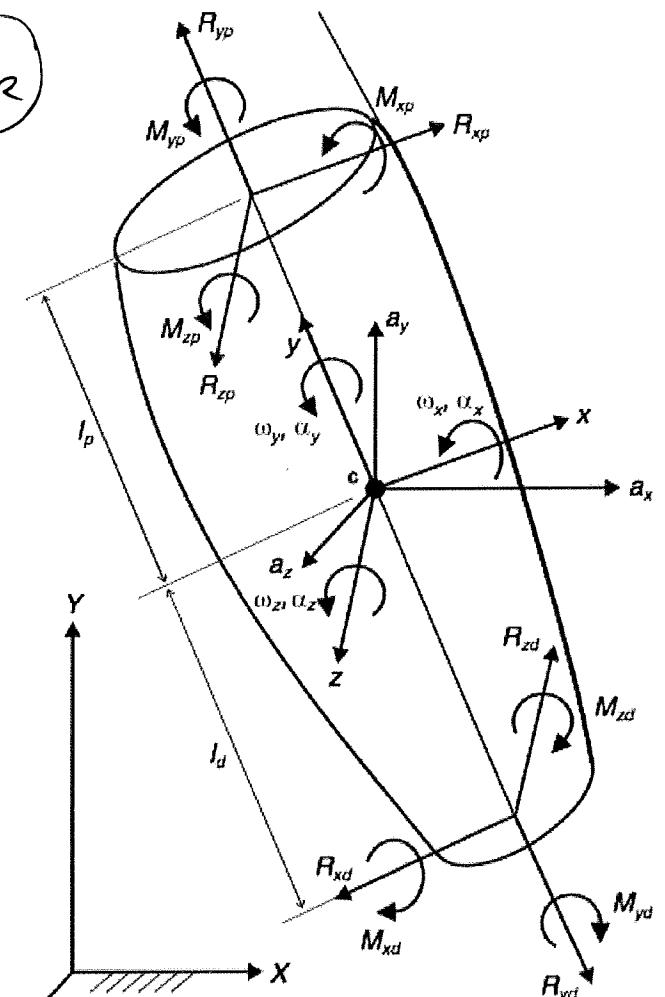
$$\sum F_z = m a_z$$

## Euler Equations

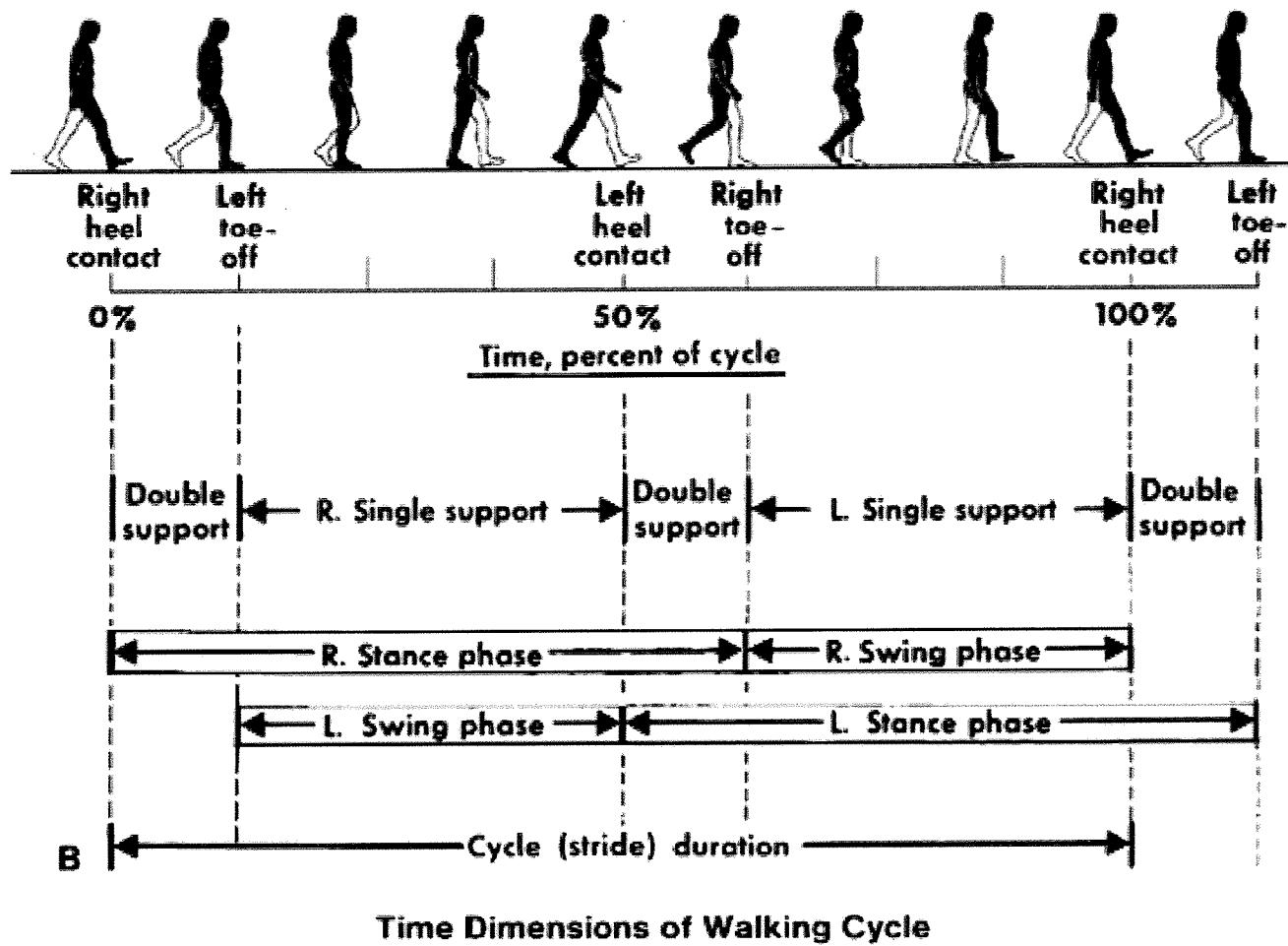
$$\sum M_x = I_x \alpha_x$$

$$+ (I_z - I_y) \omega_y \omega_z$$

Captures interaction  
of angular velocity z  
in other axes.



# The Gait Cycle



Winter, 2009

## Observation

### Phases

- \* initial contact (heel strike)
- \* loading response (weight transvers)
- \* mid stance (alignment & balance of BW.)
- \* terminal stance (heel rises) & addg power
- \* toe off (
- \* swing .

For walking the same distance compared w/  
running (70% less energy)