

Theoretical analysis of phase qubits

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Team and publications

UCR team: 1) Kyle Keane, *graduate student*
2) Dr. Ricardo Pinto, *postdoc*
3) Alexander Korotkov, *professor*

Since last review (August 2008)

Published: 3 journal papers

Submitted: 3 journal papers

1. N. Katz, M. Neeley, M. Ansmann, R. C. Bialczak, M. Hofheinz, E. Lucero, A. O'Connell, H. Wang, A. N. Cleland, J. M. Martinis, and A. N. Korotkov, "Reversal of the weak measurement of a quantum state in a superconducting phase qubit", Phys. Rev. Lett. 101, 200401 (2008).
2. A. N. Korotkov, "Quantum efficiency of binary-outcome detectors of solid-state qubits", Phys. Rev. B 78, 174512 (2008).
3. A. N. Korotkov, "Special issue on quantum computing with superconducting qubits", Quantum Inf. Process. 8, No. 2-3, 51 (2009). (Editorial paper.)
4. A.G. Kofman and A.N. Korotkov, "Two-qubit decoherence mechanisms revealed via quantum process tomography", arXiv:0903.0671.
5. A.N. Jordan and A.N. Korotkov, "Uncollapsing the wavefunction by undoing quantum measurements", arXiv:0906.3468.
6. A.N. Korotkov and K. Keane, "Decoherence suppression by uncollapsing", arXiv:0908.1134.





Research accomplishments since last review



- Analyzed tunable coupling of two phase qubits via negative mutual inductance and tunable Josephson inductance. Calculated residual coupling due to nonlinearity. Shown that ON/OFF ratio can reach 10^3 .
- Developed theory for quantum process tomography of two coupled phase qubits, including resonant ($\sqrt{i}$ swap) and detuned cases. Introduced a characteristic of decoherence non-locality. Shown ways to distinguish decoherence mechanisms using experimental χ -matrix.
- Shown that energy relaxation in phase qubits can be suppressed (theoretically almost completely) by uncollapsing procedure. Proposed demonstration experiment.
- (Editorial) As a Guest Editor of QIP, contributed to publication of the Special Issue on Quantum Computing with Superconducting Qubits.





Research topics for the next year



- Compute tunable coupling parameters using the higher order perturbation theory. Also analyze the design of tunable coupling with blocking capacitors.
- Compare efficiency of various ways of phase qubit measurement.
- Perform numerical simulations of experiments on uncollapsing with phase qubits. Analyze quantum process tomography characteristics (fidelity and elements of the χ -matrix).





Analysis of QPT (quantum process tomography) for phase qubits



Two ways: for qubits in resonance ($\sqrt{\text{iswap}}$)
and for strongly detuned qubits (simpler!)

$$H_{\text{int}} = (\hbar S / 2) \sigma_{X,1} \sigma_{X,2}$$

QPT of strongly detuned qubits

$$\chi(t) \approx \chi^I + \delta\chi^c + \lambda t$$

$$\chi_{mn}^I = \delta_{m0} \delta_{n0} \quad (\text{identity map})$$

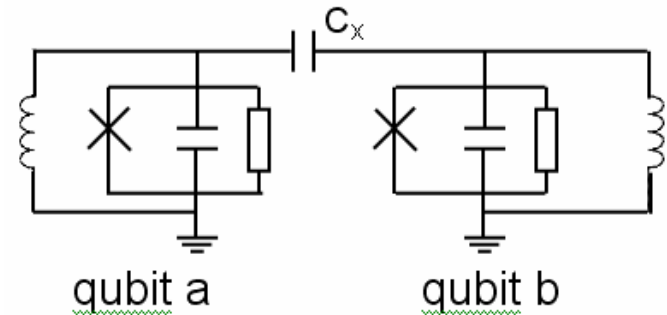
(here 0,1,2,...15 = II, IX, IY,... ZZ)

$$\delta\chi_{09}^c = \delta\chi_{60}^c = -\delta\chi_{06}^c = -\delta\chi_{90}^c = iS / 4\Delta\omega$$

(coherent evolution; small term only in the rotating frame of eigenfrequencies)

λ : matrix of Markovian decoherence

Using χ for several t , can find λ accurately and check if Markovian (by linearity in t)



Local vs. non-local decoherence
(a simple way to distinguish)

$$\text{For local: } \lambda = \lambda^{(1)} \otimes \lambda^{(2)}$$

Decoherence non-locality parameter:

$$\epsilon_{NL} = \frac{\text{Tr} |\lambda - \tilde{\lambda}|}{\text{Tr} |\lambda|}$$

$$\tilde{\lambda} = \tilde{\lambda}^{(1)} \otimes \chi^{I(2)} + \chi^{I(1)} \otimes \tilde{\lambda}^{(2)},$$

$$\tilde{\lambda}^{(1,2)} = \text{Tr}_{2,1} \lambda, \quad |A| = \sqrt{A^\dagger A},$$

Kofman & Korotkov, arXiv:0903.0671





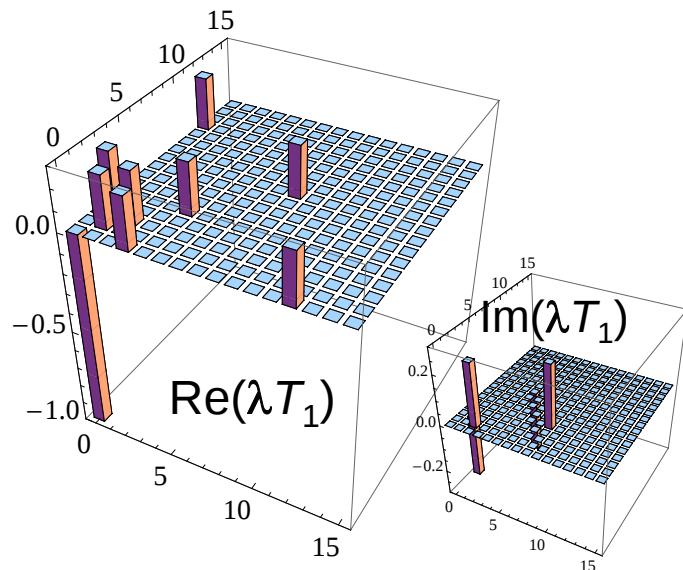
λ -matrix for several decoherence mechanisms



$$\lambda = \lambda_{\text{EnRel}} + \lambda_{\text{CorrPD}} + \lambda_{\text{NoisyCpl}}$$

Energy relaxation

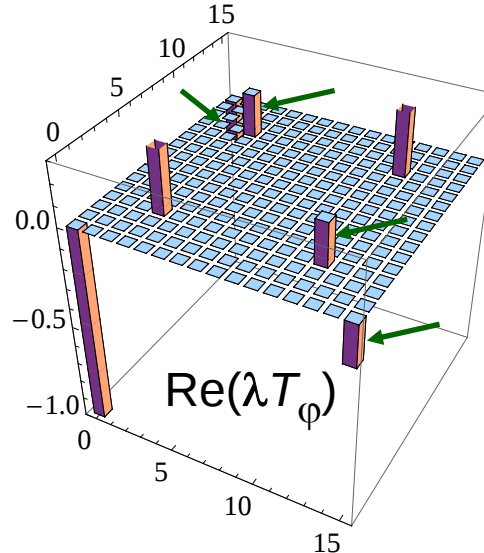
$$\begin{aligned}\lambda_{00} &= -1/2T_1^{(1)} - 1/2T_1^{(2)} \\ \lambda_{11} &= \lambda_{22} = 1/4T_1^{(2)}, \lambda_{44} = \lambda_{88} = 1/4T_1^{(1)} \\ \lambda_{03} &= \lambda_{30} = 1/4T_1^{(2)}, \lambda_{0,12} = \lambda_{12,0} = 1/4T_1^{(1)} \\ \lambda_{21} &= -\lambda_{12} = i/4T_1^{(2)}, \lambda_{84} = -\lambda_{48} = i/4T_1^{(1)}\end{aligned}$$



Partially correlated (nonlocal) dephasing

$$\begin{aligned}\lambda_{00} &= -1/2T_\varphi^{(1)} - 1/2T_\varphi^{(2)} \\ \lambda_{33} &= 1/2T_\varphi^{(2)}, \lambda_{12,12} = 1/2T_\varphi^{(1)} \\ \lambda_{3,12} &= \lambda_{12,3} = -\lambda_{0,15} = -\lambda_{15,0} \\ &= \kappa / 2\sqrt{T_\varphi^{(1)}T_\varphi^{(2)}}\end{aligned}$$

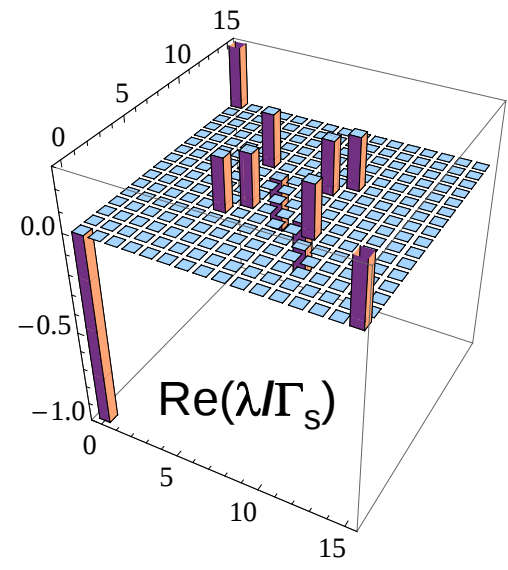
κ - correlation factor



Specific pattern for each mechanism!

Noisy coupling (slightly different than in resonance)

$$\begin{aligned}\lambda_{00} &= -\Gamma_s, \quad \lambda_{0,15} = \lambda_{15,0} = \Gamma_s / 2 \\ \lambda_{55} &= \lambda_{10,10} = \lambda_{5,10} = \lambda_{10,5} = \Gamma_s / 4 \\ \lambda_{66} &= \lambda_{99} = -\lambda_{69} = -\lambda_{96} = \Gamma_s / 4\end{aligned}$$

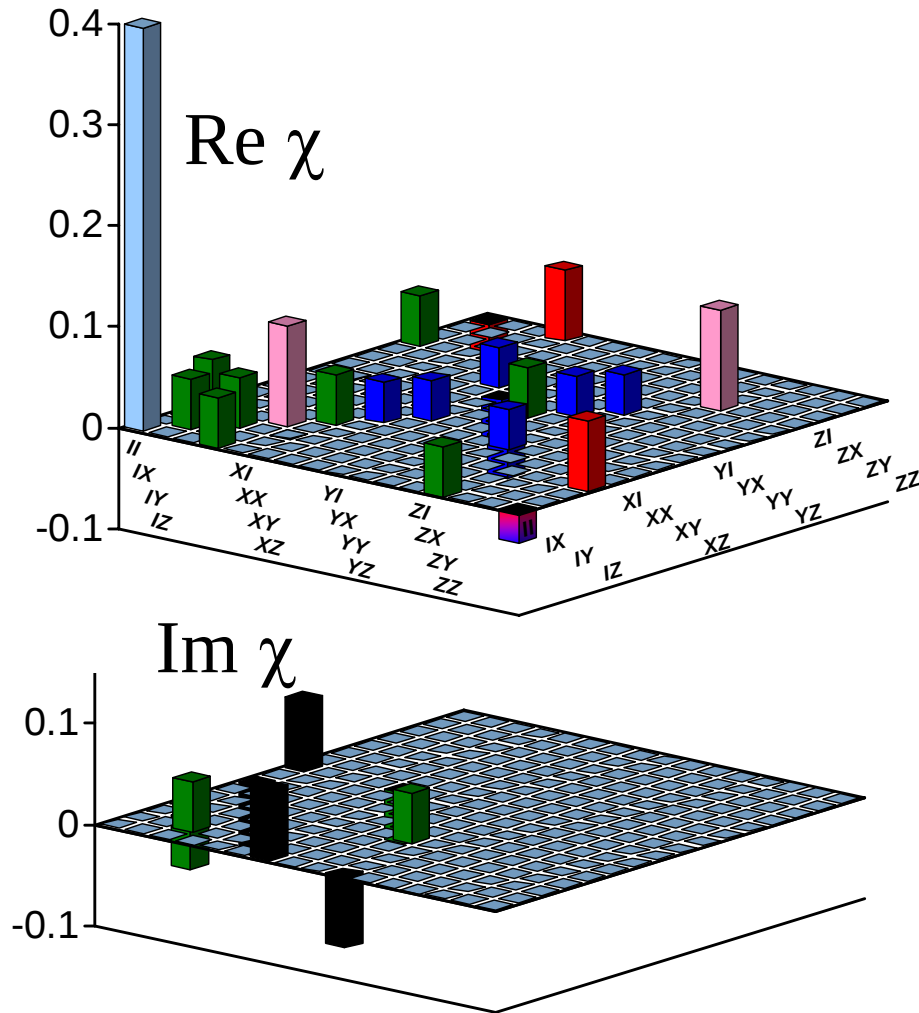


All positions (except 00=11,11) are also different from χ' and $\delta\chi^c$





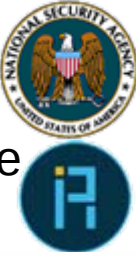
χ -matrix for strongly detuned qubits



- Identity mapping
- Remaining unitary evolution
- Energy relaxation
- Uncorrelated pure dephasing
- Correlated (non-local) pure dephasing
- Noisy coupling

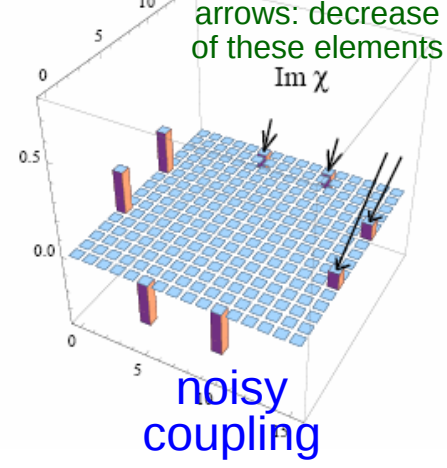
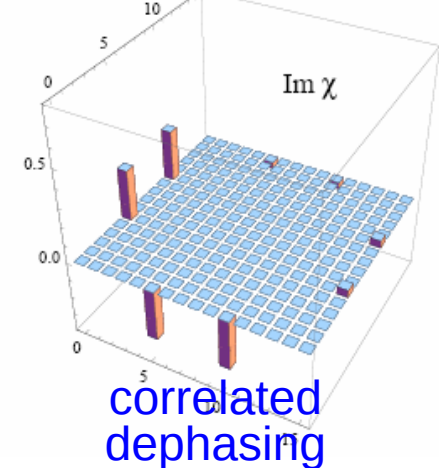
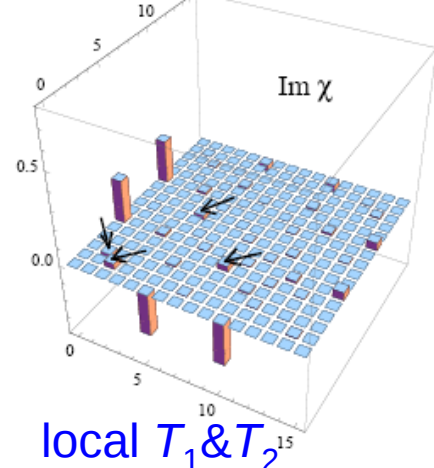
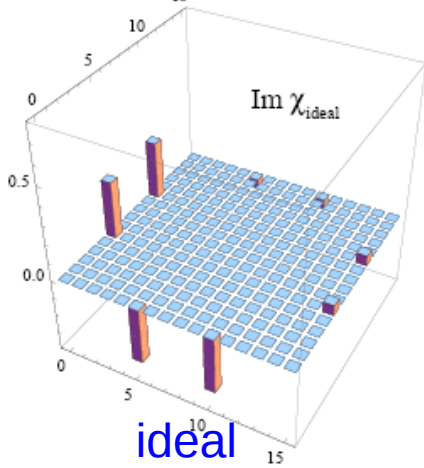
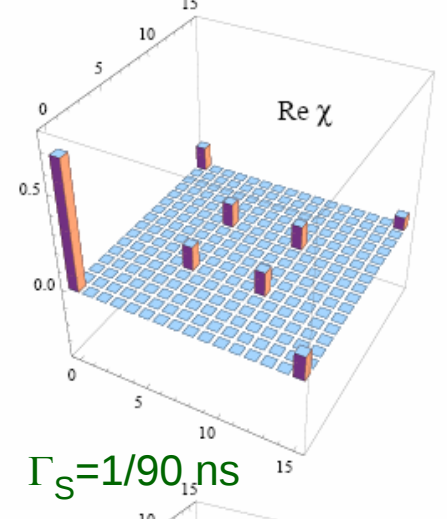
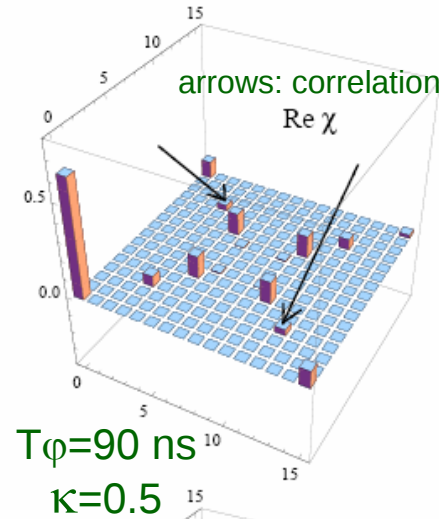
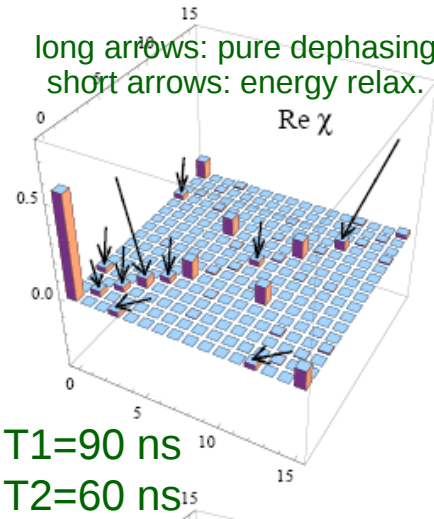
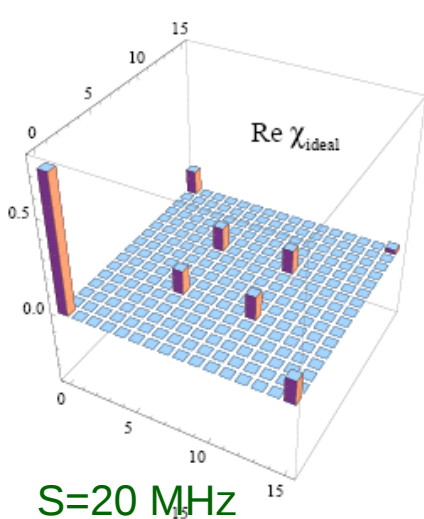
very simple to distinguish
decoherence mechanisms





If qubits are in resonance, then not so easy: $\chi \neq \chi_{ideal} + \lambda t$

However, for $\sqrt{\text{iswap}}$ and for largest extra elements of χ , it is still a simple addition, that makes distinguishing decoherence mechanisms quite easy



Interesting to compare decoherence data from resonant and strongly detuned qubits

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Kofman & Korotkov, arXiv:0903.0671

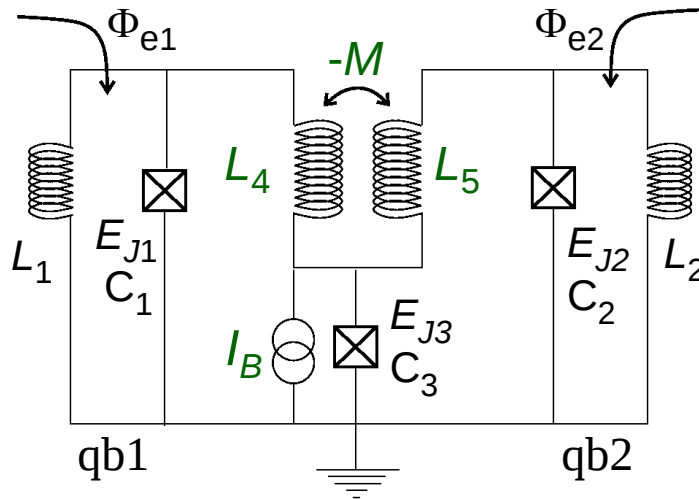
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Tunable coupling of phase qubits

Pinto & Korotkov, in preparation



$$H_{\text{int}} = \frac{\hbar \Omega_C}{2} \sigma_{X,1} \sigma_{X,2} + \underbrace{\hbar \Omega_{ZZ} \sigma_{Z,1} \sigma_{Z,2}}_{\text{small unwanted term due to non-linearity}}$$

Ω_C can be tuned by bias current I_B

physically:

$$H_{\text{int}} = \frac{M}{L_4 L_5} \delta \Phi_1 \delta \Phi_2 - \frac{1+M/L_5}{L_4} \delta \Phi_1 \delta \Phi_3 - \frac{1+M/L_4}{L_5} \delta \Phi_2 \delta \Phi_3$$

then perturbation theory, with account of non-linearity in qubits and coupling

$$\Omega_C = \frac{1}{L_4 L_5 \omega_{qb} \sqrt{C_1 C_2}} \left(M - \frac{L_{JC}}{1 - (\omega_{qb} / \omega_3)^2} \right)$$

$$\Omega_{ZZ} = \frac{b_1 b_2 / 8}{L_4 L_5 \omega_{qb} \sqrt{C_1 C_2}} (M - L_{JC})$$

- main coupling Ω_C can be zeroed exactly
- unwanted coupling Ω_{ZZ} is much smaller ($\times b_1 b_2 / 8$)
- coupling Ω_{ZZ} also crosses zero at a close point

where $b = \frac{\langle 1 | \phi | 1 \rangle - \langle 0 | \phi | 0 \rangle}{\langle 1 | \phi | 0 \rangle} \approx \frac{1}{\sqrt{3 N_{\text{levels}}}}$, $L_{JC} = \frac{(1+M/L_4)(1+M/L_5)}{\omega_3^2 C_3} \approx \frac{\Phi_0 / 2\pi}{\sqrt{I_{\text{crit},3}^2 - I_B^2}}$

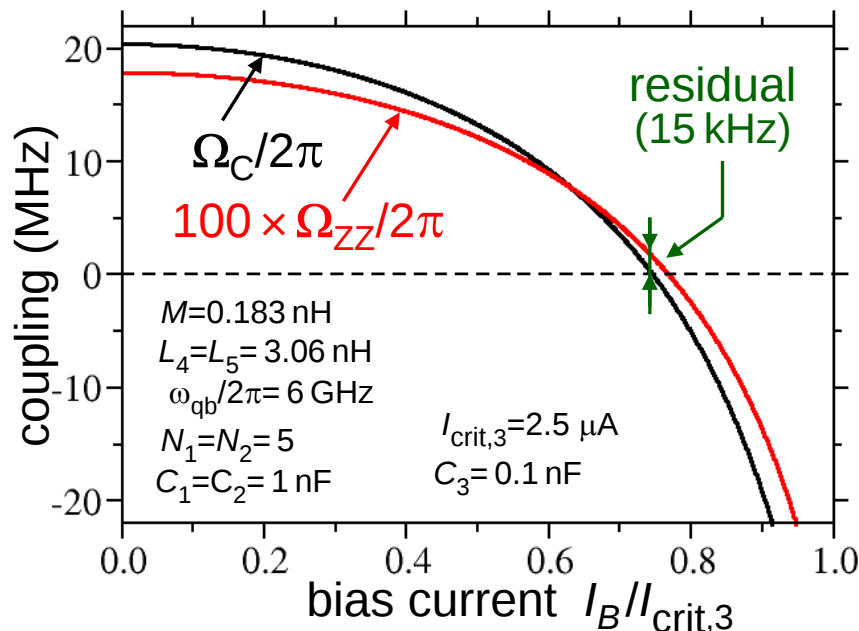
(ratio ω_{qb}/ω_3 is arbitrary)





Residual coupling

Simulation using experimental parameters



Ω_{ZZ} is unpleasant but not dangerous, can be compensated algorithmically. Important for QC is how well the total coupling can be zeroed.

Residual coupling: Ω_{ZZ} when $\Omega_C=0$

$$\Omega_{ZZ}^{\text{res}} = \frac{b_1 b_2}{8} \frac{M}{L_4 L_5 \omega_{qb} \sqrt{C_1 C_2}} \left(\frac{\omega_{qb}}{\omega_3} \right)^2$$

Nonlinearity in the coupling junction gives some corrections, but not quite important, main effect is due to nonlinearity in the qubits.

Still need to do:

- next order perturbation theory; it may affect residual coupling
- beyond-RWA corrections

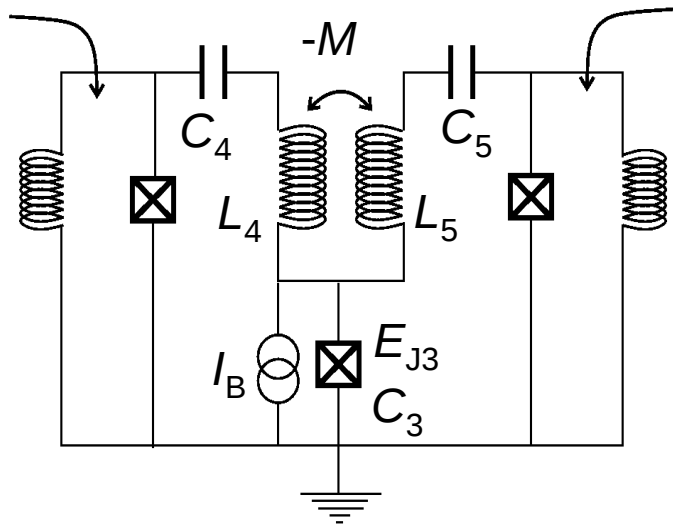
$$\frac{\text{OFF}}{\text{ON}} \approx \frac{b_1 b_2}{4} \left(\frac{\omega_{qb}}{\omega_3} \right)^2 \approx \frac{1}{12 N_{\text{levels}}} \left(\frac{\omega_{qb}}{\omega_3} \right)^2 \sim 10^{-3}$$

Pinto & Korotkov, in preparation





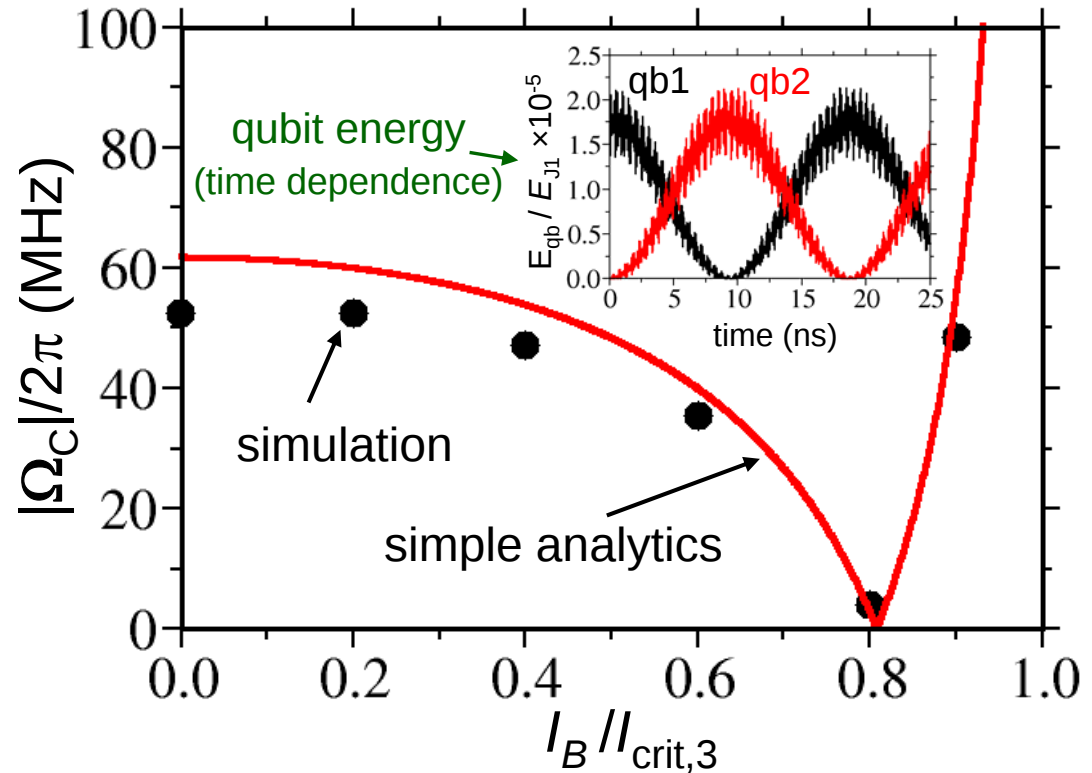
Another design of tunable coupling



From simple circuit analysis:

$$\Omega_C \approx (M - L_{JC}) \frac{C_4 C_5}{\sqrt{C_1 C_2}} \omega_{qb}^3$$

$$L_{JC} \approx \frac{\Phi_0 / 2\pi}{\sqrt{I_{crit,3}^2 - I_B^2}}$$



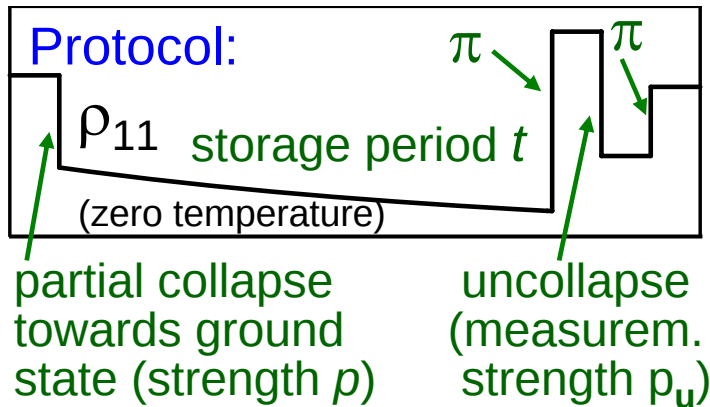
- Classical coupling simulated numerically; results close to what was expected
- Quantum coupling still to be analyzed (in progress)





Suppression of T_1 -decoherence by uncollapsing

Korotkov & Keane,
arXiv:0908.1134



(almost same as existing experiment!)

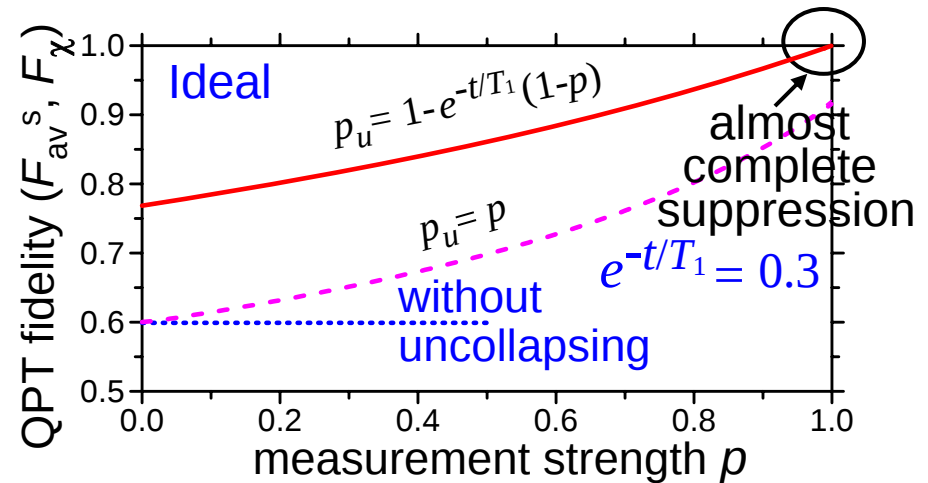
Ideal case (T_1 during storage only)

for initial state $|\psi_{in}\rangle = \alpha |0\rangle + \beta |1\rangle$

$|\psi_f\rangle = |\psi_{in}\rangle$ with probability $(1-p)e^{-t/T_1}$

$|\psi_f\rangle = |0\rangle$ with $(1-p)^2|\beta|^2 e^{-t/T_1}(1-e^{-t/T_1})$

procedure preferentially selects
events without energy decay



(Actually, QPT fidelity is not directly applicable to algorithms with selection (including linear optics QC); however, we have shown that “naïve” QPT fidelity is still very close to the scaled average state fidelity.)

Dynamical decoupling (NMR-like) cannot protect against T_1 -decoherence, so uncollapsing is **the only** known to us way to protect without encoding in a larger Hilbert space (QEC, DFS)





Suppression of T_1 -decoherence by uncollapsing (cont.)



Analytics for the ideal case

Average state fidelity

$$F_{av} = \frac{1}{2} + \frac{1}{C} + \frac{\ln(1+C)}{C^2}$$

“Naïve” QPT fidelity

$$F_{\chi} = -\frac{1}{4} + \frac{1}{4(1+C)} + \frac{4+C}{2(2+C)}$$

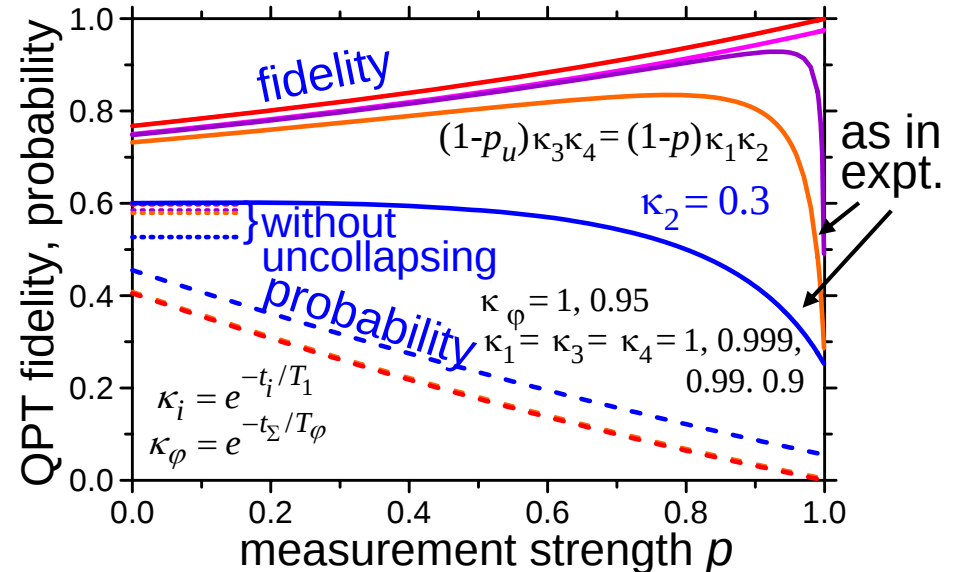
$$F_{\chi} \approx \frac{3F_{av} - 1}{2} \quad (\text{very close})$$

where $C = (1-p)(1-e^{-\Gamma t})$

$$p_u = 1 - e^{-\Gamma t}(1-p)$$

Trade-off: larger p gives stronger decoherence suppression, but smaller selection probability

Realistic case (T_1 and T_{ϕ} at all stages)



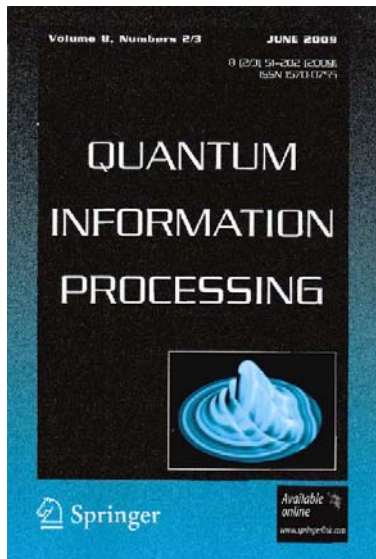
- decoherence due to pure dephasing is not affected
- T_1 -decoherence between first π -pulse and second measurement causes decrease of fidelity at p close to 1

Korotkov & Keane, arXiv:0908.1134





(Advertisement)



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(June 2009)
Special Issue
on QC with
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The latest comprehensive collection of review papers on experimental Quantum Computing with Superconducting Qubits

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